

01. SOLUTIONS (Sem-01)

Homogenous mixture of two or more substances is called solution. The substance which is present in large proportion is termed the 'Solvent' while the other which is present in smaller proportion is called 'Solute'.

Types of solutions:- depending upon the physical state of the solute & the solvent, binary solutions are divided into 9 types.

Types of Solutions

solute	solvent	Example.
(i) Solid	liquid	Salt or sugar in water
(ii) Liquid	Liquid	Alcohol in water
(iii) Gas	Liquid	soda water (CO_2 in H_2O)
(iv) Solid	Solid	Alloys like brass, bronze etc.
(v) Liquid	Solid	Hydrates, jellies.
(vi) Gas	Solid	Dissolved gases in transition metals & minerals; (e.g. Hydrogen in palladium).
(vii) Solid	Gas	Smoke (carbon particles in air)
(viii) Liquid	Gas	Moisture in air
(ix) Gas	Gas	Water vapour in air (humidity), cooking gas, air.

Azeotropic mixture :- "A mixture of 2 or more liquids which boils at a constant temperature and distills over completely at the same temperature without change in composition is known as "Azeotropic Mixture".

Azeotropic mixtures although boil at a constant temperature.

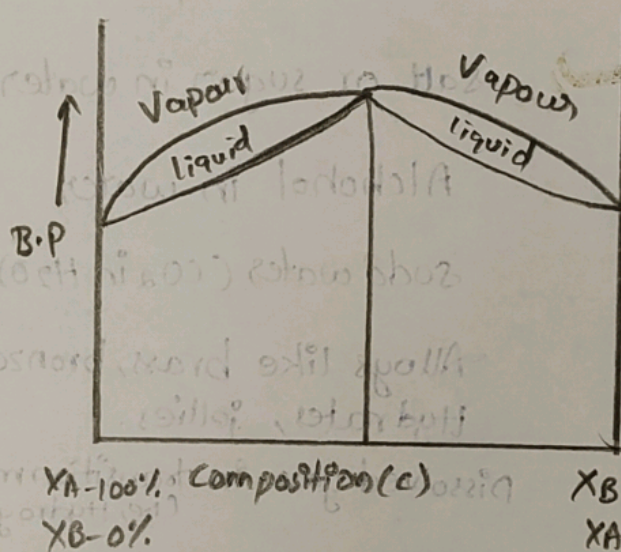
Azeotropic mixtures are of two types:

- 1) maximum azeotropic mixtures
- 2) minimum azeotropic mixtures.

(1) Maximum Azeotropic mixtures: The Boiling point of Azeotropic is more than that of its composition. These mixtures shows deviations from Raoult's law.

The mixture which evaporates at max. boiling point without changing their composition at constant temperature is known as "Maximum Azeotropic mixtures".

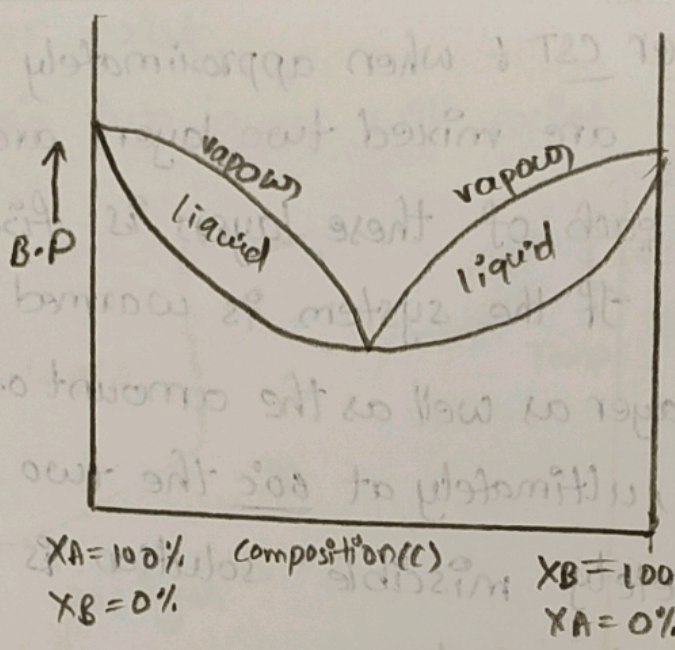
Ex: Max. Boiling point of $\text{HCl} + \text{H}_2\text{O}$ is 108.5°C.



(2) Minimum Azeotropic Mixtures: The Boiling point of the azeotropic mixture is less than that of its compositions. These mixture shows positive deviations from Raoult's law.

The mixture which evaporates at minimum boiling point without changing their composition at constant temperature is known as "minimum azeotropic mixtures".

Ex: The B.P of $\text{C}_2\text{H}_5\text{OH} + \text{H}_2\text{O}$ is 98.1°C



Partially Miscible Liquids: There are number of liquid pairs which are only partially miscible with one another. If a little amount of phenol (or) aniline (or) ether is added to water at ordinary temperature. It will dissolve completely but if the addition is continued a state is reached when no further dissolution occurs and the two liquid layers are formed.

"The solutions of different compositions co-existing with one another are termed "conjugate solutions".

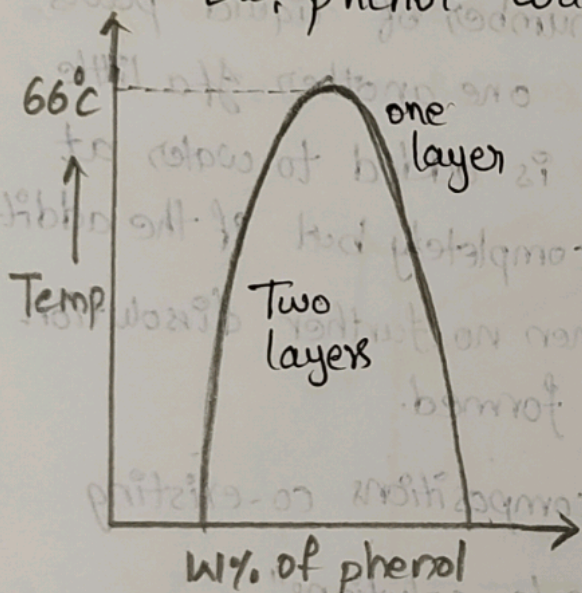
Critical solution temperature (CST):- The temperature at which the two partially miscible liquids become completely miscible is called "Critical solution temperature (or) consolute temperature of the system.

partially miscible liquids may be classified into 3 types depending upon their CST.

- (i) partially miscible liquids having upper CST
- (ii) partially miscible liquids having lower CST.
- (iii) partially miscible liquids having upper & lower CST

i) System with an upper CST : When approximately equal amounts of phenol in water are mixed two layers are produced. The composition of each of these layers is fixed at a given temperature. If the system is warmed the amount of phenol in water layer as well as the amount of water in phenol layer increase, ultimately at 66°C the two layers become the same and completely miscible solution is formed.

Ex: phenol-water system.



⇒ The plot leads to the following conclusions:
 ⇒ At and above 66°C phenol and water are completely miscible, whatever may be their composition.
 ⇒ At any temperature below 66°C the composition of the system lies in the range of the curve.

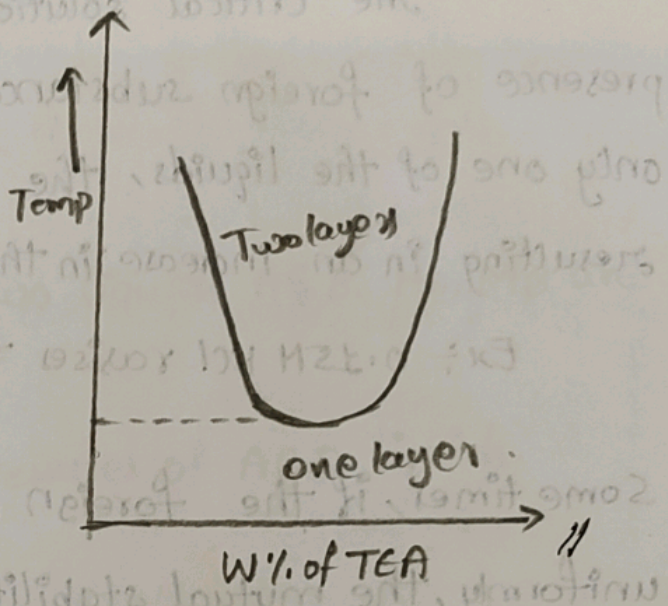
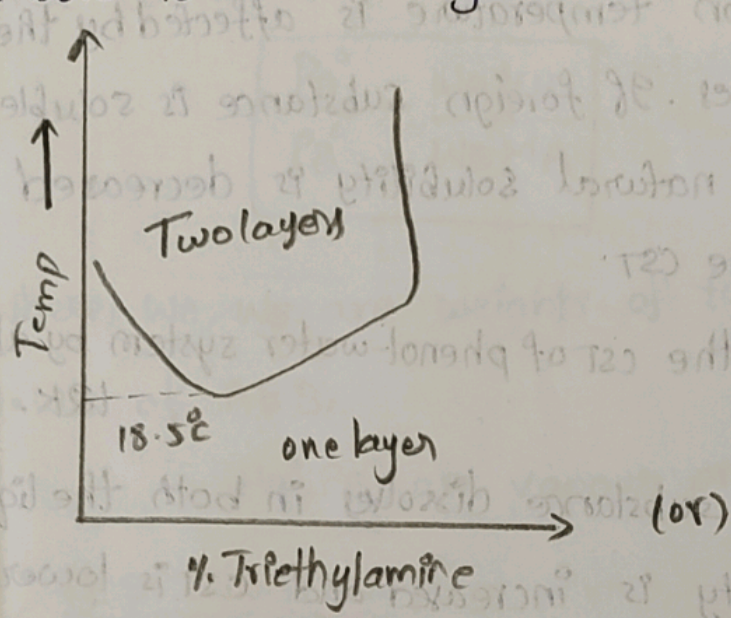
(ii) System with Lower CST : When approximately equal amounts of Triethylamine (TEA) and water are mixed, a partially miscible solution is formed. The mutual solubility of the liquids increases with decrease in temperature. Thus, cooling the system to 18.5°C causes the two components to become completely miscible with each other, so, this temperature is called lower consolute temperature.

Ex: Triethylamine - water.

⇒ At and below 18.5°C the two liquids are completely miscible in all proportions. i.e., the system is homogeneous.

only one layer exist.

Above 18.5°C two layers will exist.

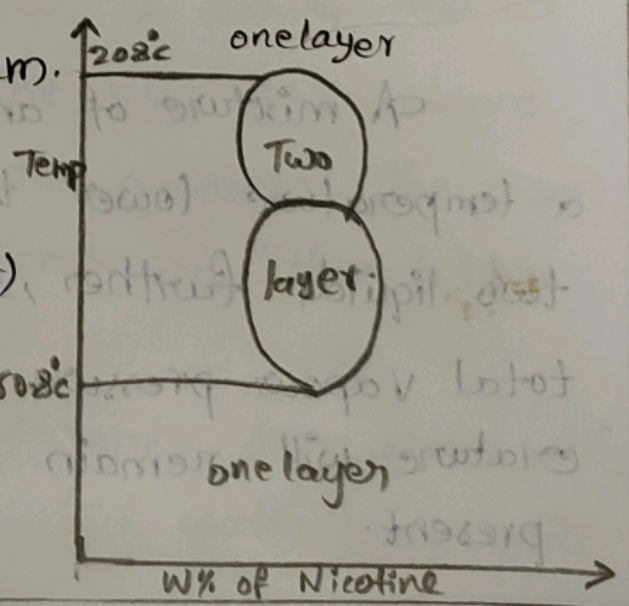


1) System with an upper and lower CST: In this type of system the natural solubility of the two liquids increases with increase of temperature as well as decrease of temperature.

At normal temperature, when an approximately equal amount of Nicotin in water are mixed, a partially miscible liquid is formed. when temperature raises to 20.8°C (or) decrease to 60.8°C causes the completely miscible solutions. Hence, these two temperatures are maximum CST and minimum CST respectively.

Ex: Nicotine - water system.

These liquids are miscible at a certain higher temp (upper CST) as well as at a certain lower temp (Lower CST). Btw these two limiting temperature, they are partially miscible.



Effect of impurity on consolute temperature:

The critical solution temperature is affected by the presence of foreign substances. If foreign substance is soluble only one of the liquids, the natural solubility is decreased resulting in an increase in the CST.

Ex: 0.15M KCl raises the CST of phenol-water system by 12K.

Sometimes, if the foreign substance dissolves in both the liquids uniformly, the mutual stability is increased and CST is lowered.

Ex: 0.083M sodium oleate decreases the CST of phenol-water system to 329.7K.

Completely immiscible liquids: Immiscible liquids are those which do not mix with each other at all. In these liquids, each component liquid exerts its own vapour pressure independent of the presence of the other. Hence total vapour pressure is the sum of the two pure constituents.

$$P = P_A + P_B$$

P_A & P_B are the vapour pressures of pure liquids A & B respectively at the same temperature.

A mixture of any two immiscible liquids will boil at a temperature lower than the boiling point either of the two liquids further, since, when the mixture is boiling, the total vapour pressure remains the same, the boiling temperature will remain constant so long both liquids are present.

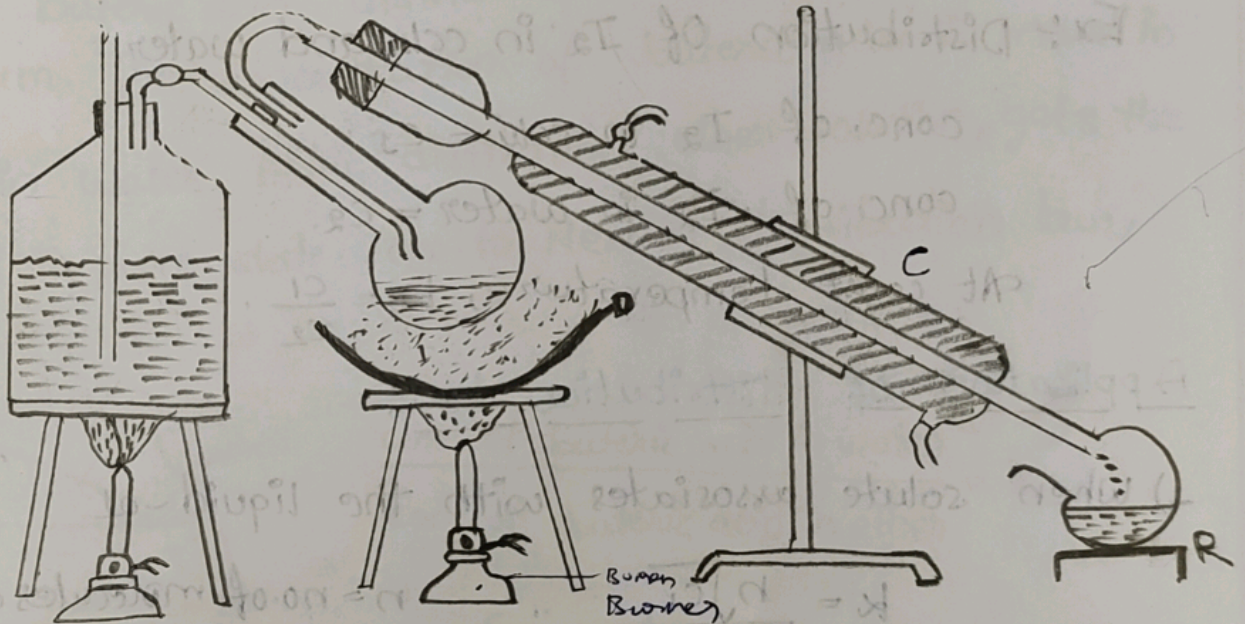
The relative proportions of the two liquids in the distillate can be calculated as partition of efficient:

$$\frac{P_A^\circ}{P_B^\circ} = \frac{W_A M_B}{W_B M_A}$$

Where, W_A, W_B are weights of two liquids A & B. M_A, M_B are M.wts of A & B,

P_A°, P_B° are vapour pressures of A & B liquids.

DISTILLATION:-



As in the above distillation diagram the flask containing impure liquid to be purified is slowly heated and a current of steam picks up the volatile substance from the liquid and passes it in to the condenser. The steam liquid vapours condense in the condenser and thus trickle down in the receiver.

The pure liquid is then separated from water with the help of a separating funnel in which water and liquid

(pure) form two separate layers and hence collected separately.

The relative amounts of the organic substance and water in the distillate depend on their molecular weights and water vapour pressures at the boiling point.

$$\frac{\text{weight of distilled water}}{\text{weight of substance distilled}} = \frac{M_{\text{w}} \text{ of } H_2O \times \text{part. press. of water}}{M_{\text{w}} \text{ of substance} \times \text{partial press. of substance}}$$

Nernst Distribution law:

"At constant temperature, a solute distributes itself between two miscible solvents only in a particular ratio."

Ex:- Distribution of I_2 in CCl_4 and water.

$$\text{conc. of } I_2 \text{ in } CCl_4 = c_1$$

$$\text{conc. of } I_2 \text{ in water} = c_2$$

$$\text{At const temperature, } K_D = \frac{c_1}{c_2}$$

Application of distribution law:

1) When solute associates with the liquid-01

$$K = \frac{n \sqrt{c_1}}{c_2}$$

n = no. of molecules associated

c_1 = con. of solute in liq-01

c_2 = con. of solute in liq-02

K = dissociation constant

2) When solute associates with liquid-02.

$$K = \frac{c_1}{n \sqrt{c_2}}$$

3) When solute dissociates in liquid-01

$$K = \frac{c_1(1-\alpha)}{c_2}$$

α = extent of dissociation

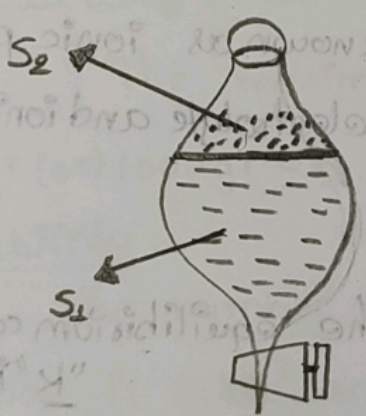
4) When solute dissociate in both the solvents,

$$k = \frac{c_1(1-\alpha_1)}{c_2(1-\alpha_2)}$$

Application of Nernst distribution law in solvent extraction:-

If an organic compound is distributed in an organic solvent and water, that substance is more soluble in organic solvent while less in water.

Ex: Buteric acid is distributed in water and ether. Take the above mixture in a separating funnel and shake it. After some time buteric acid distributes in both the solutions, and equilibrium. The concentration of buteric acid is more in ether than in water. After distillation ether solution, gets the buteric acid in pure state. acc. to Nernst's distribution law,



$$\frac{\text{conc. of buteric acid in water}}{\text{conc. of buteric acid in ether}} = K_D$$

S₁ = water phase

S₂ = organic phase

Limitations of distribution law :-

- 1) This law applicable at const temperature only.
- 2) Solute must distributes in two solutions equally.
- 3) Solute neither associates nor dissociates with either of solvents.
- 4) Two solvents must be immiscible.

SHORT QUESTIONS

- 01) what are azeotropes? and explain HCl-H₂O₂ and ethanol-water system?
- 02) write the effect of impurity on consolute temperature

LONG QUESTIONS

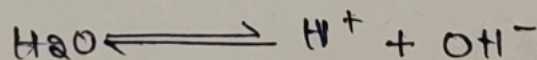
- 01) write about steam distillation.
- 02) write the definition and types of azeotropic mixtures.
- 03) what is Nernst distribution law and its applications.

2. IONIC EQUILIBRIUM

Ionic product :- The product of concentrations of cation and anion at a particular temperature is called ionic product.

Ionic product of water :-

The product of concentrations of H⁺ and OH⁻ ions in water at a particular temperature is known as ionic product of water. pure water is a very weak electrolyte and ionises



According to law of mass action. The equilibrium constant "K" is

$$K = \frac{[\text{H}^+][\text{OH}^-]}{[\text{H}_2\text{O}]}$$

$$\Rightarrow K[\text{H}_2\text{O}] = [\text{H}^+][\text{OH}^-]$$

But, $K[\text{H}_2\text{O}] = K_w$ then

$$\boxed{K_w = [\text{H}^+][\text{OH}^-]}$$

Where, K_w = Ionic product of water.

The value of K_c increases with temperature
units of $K_w = \text{mole}^2 \text{lit}^{-2}$

since, pure water is neutral $[\text{H}^+] = [\text{OH}^-]$

$$K_w \text{ at } 25^\circ\text{C} = 1.0 \times 10^{-14} (\text{mole/lit})^2$$

$$\textcircled{1} \quad K_w \text{ at } 10^\circ\text{C} = < 1.0 \times 10^{-14} (\text{mole/lit})^2$$

$$K_w \text{ at } 50^\circ\text{C} = > 1.0 \times 10^{-14} (\text{mole/lit})^2$$

The solution will be acidic in nature, when $[\text{H}^+] > [\text{OH}^-]$ then,

$$[\text{H}^+] > 1.0 \times 10^{-7} \text{ M} \quad (\text{M} = \text{molar})$$

$$[\text{OH}^-] < 1.0 \times 10^{-7} \text{ M}$$

The solution will be basic in nature, when $[\text{OH}^-] > [\text{H}^+]$ then,

$$[\text{OH}^-] > 1.0 \times 10^{-7} \text{ M}$$

$$[\text{H}^+] < 1.0 \times 10^{-7} \text{ M}$$

⁽²⁾
Solubility \div $\textcircled{1}$

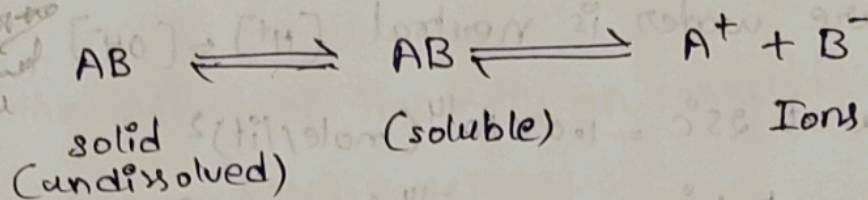
The maximum amount of salt that can dissolve in 100gr (or) 1000gr of solvent at room temperature is called its solubility.

The number of moles of solute dissolved in one litre of solution is called molar solubility. The sparingly soluble salts are almost insoluble.

The solution containing the salt dissolved state in an amount which is greater than the solubility amount of the salt at room temperature is called saturated solution. A saturated solution contains salt in the solid form and in dissolved form. Hence, there exist two dynamic equilibria in the solution.

Dissolved salt \rightleftharpoons ion of the salt

Undissolved salt \rightleftharpoons dissolved salt



(2) The categories of salts based on their solubility in

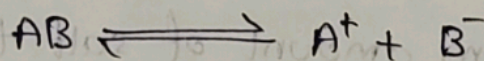
if solubility $> 0.1M$ \longrightarrow salt is highly soluble

solubility $< 0.1M$ \longrightarrow sparingly soluble.

$0.01 < \text{solubility} < 0.1M$ \longrightarrow slightly soluble.

Solubility product (K_{sp}) :-

"The product of the ionic concentration in a saturated solution of a soluble electrolyte at constant temperature is called solubility product."

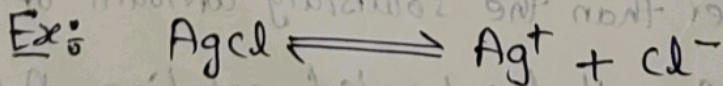


$$K = \frac{[A^+][B^-]}{[AB]}$$

$$K[AB] = [A^+][B^-]$$

$$\text{But } K[AB] = K_{sp}$$

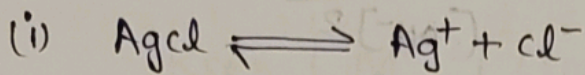
$$\text{Then } K_{sp} = [A^+][B^-]$$



$$K_{sp} = [Ag^+][Cl^-]$$

Solubility of $AgCl$ is low in concentrated solution.

RELATION BETWEEN SOLUBILITY (S) AND SOLUBILITY PRODUCT (K_{sp})



$$K = \frac{[\text{Ag}^+][\text{Cl}^-]}{[\text{AgCl}]}$$

Relation

$$K_{sp} = x^x \cdot y^y \cdot s^{x+y}$$

$$K_{sp} = [\text{Ag}^+][\text{Cl}^-] \quad (3)$$

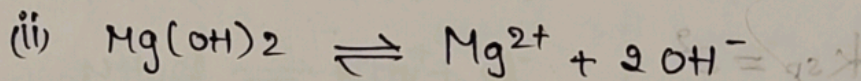
if the solubility of $[\text{Ag}^+] = S$

and if the solubility of $[\text{Cl}^-] = S$

then, $K_{sp} = [\text{Ag}^+][\text{Cl}^-]$

$$K_{sp} = S \cdot S$$

$$\therefore \boxed{K_{sp} = S^2}$$



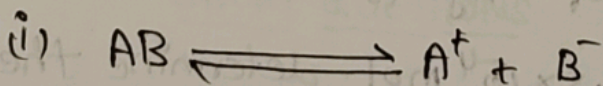
$$K_{sp} = [\text{Mg}^{2+}][\text{OH}^-]^2$$

$$= S \cdot (2S)^2 \Rightarrow S \cdot 4S^2$$

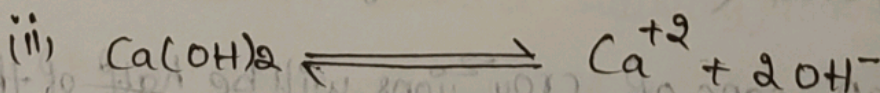
$$\boxed{K_{sp} = 4S^3}$$

Calculations based on solubility product

Some times an ion remains after precipitation if it is in excess. Remaining concentration can be determined as.



$$[\text{A}^+]_{\text{left}} = \frac{K_{sp}(\text{AB})}{[\text{B}^-]}$$



$$[Ca^{+2}]_{left} = \frac{K_{sp} [Ca(OH)_2]}{[OH^-]^2}$$

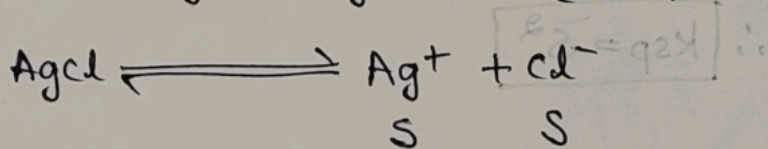
(iii) percentage precipitation of anion.

$$= \left[\frac{\text{Initial concentration} - \text{left concentration}}{\text{Initial concentration}} \right] \times 100$$

PROBLEMS

(1) The solubility product of silver chloride is 1.5625×10^{-10} at $25^\circ C$.
 its solubility.

(A) Let, the solubility of AgCl be S (mole/lit)



$$K_{sp} = S^2$$

$$1.5625 \times 10^{-10} = S^2$$

$$S = 1.25 \times 10^{-5} \text{ mol/lit.}$$

$$\text{M.wt of AgCl} = 143.5$$

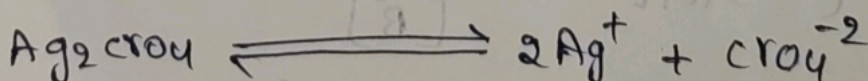
$$\text{solubility} = \text{M.wt} \times S$$

$$= 143.5 \times 1.25 \times 10^{-5}$$

$$= 1.79 \times 10^{-3} \text{ g/lit.}$$

(2) The concentrations of Ag^+ ion in a saturated solution of Ag_2CrO_4 at $20^\circ C$ is 1.5×10^{-4} mol. determine the K_{sp} of Ag_2CrO_4 at $20^\circ C$.

sol.



acc. to eqn. conc of CrO_4^{2-} ions will be half of the conc. Ag^+

$$[Ag^+] = 1.5 \times 10^{-4} \text{ m} \quad [CrO_4^{2-}] = 0.75 \times 10^{-4} \text{ m}$$

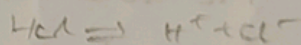
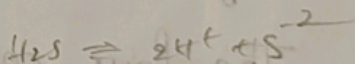
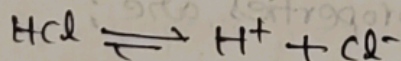
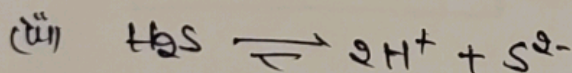
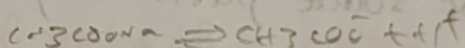
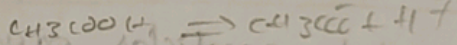
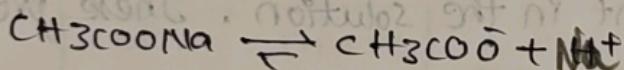
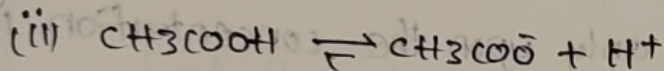
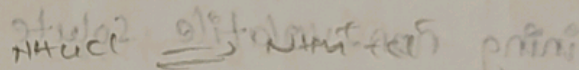
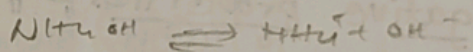
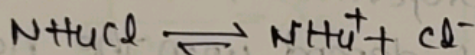
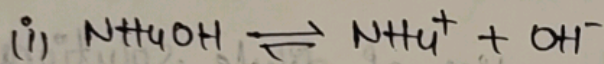
$$K_{sp} = [Ag^+]^2 [CrO_4^{2-}]$$

$$= (1.5 \times 10^{-4})^2 (0.75 \times 10^{-4})$$

$$K_{sp} = 1.6875 \times 10^{-12}$$

Common ion effect: "decrease in ionisation of weak electrolyte caused by the addition of a strong electrolyte having an ion common with weak electrolyte"

Ex: decrease of ionisation of NH_4OH ($(NH_4)_2CO_3$) in presence of NH_4Cl , CH_3COOH in presence of CH_3COONa and H_2S in presence of HCl .



Common ion effect is of great importance in analytical chemistry, especially in qualitative and quantitative analysis.

SHORT QUESTIONS

1. Explain about ionic product of water.
2. Write a short notes on solubility.
3. Write the calculations based on solubility product.
4. Explain about common ion effect.

LONG QUESTIONS

Q1. What is solubility product and explain the relation between solubility (s) and solubility product (K_{sp}).

03. DILUTE SOLUTIONS

A solution may be defined as a homogeneous mixture of two or more substances. The substance which is to be dissolved is called a solute, while the medium in which the solute is dissolved to get a homogeneous solution is called the solvent. A solution in which a small amount of solute is present is called a dilute solution, while a large amount of the solute is present is called a concentrated solution.

* Colligative properties: "The properties of dilute solutions containing non-volatile solute do not depend upon the nature of solute dissolved but depend only upon the concentration, i.e. no. of solute particles present in the solution. These properties are called colligative properties."

The four colligative properties are:

- 1) Lowering of vapour pressure
- 2) Elevation in boiling point
- 3) Depression in freezing point
- 4) Osmotic pressure.

(1) Lowering of vapour pressure: When a non-volatile solute is dissolved in the pure solvent (liquid), the vapour pressure of the liquid is lowered. The vapour pressure of the solution will be less than that of the pure solvent.

If p^0 is the vapour pressure of the solvent and p is the vapour pressure of the solution.

lowering of vapour pressure $= p^0 - p$

Relative lowering of vapour pressure and Raoult's Law :-

The ratio of lowering of vapour pressure to the vapour pressure of pure solvent is called the relative lowering of vap.

$$\text{Relative lowering of vapour pressure} = \frac{p^0 - p}{p^0}$$

Raoult's Law :- "The relative lowering of vapour pressure of a dilute solution containing non volatile solute is equal to the mole fraction of the solute present in the solution."

$$\frac{p^0 - p}{p^0} = X_2$$

$$X_2 = \text{mole fraction of solute} = \frac{n_2}{n_1 + n_2}$$

$$\frac{p^0 - p}{p^0} = \frac{n_2}{n_1 + n_2}$$

$\Rightarrow n_2 = \text{no. of moles of a solute.}$

where, $p^0 =$ Vapour pressure of pure solvent.

$p =$ Vapour pressure of solution.

$n_1 =$ no. of moles of solvent

$n_2 =$ no. of moles of solute.

In dilute solution quantity of solute is less. Hence, neglect its value from the denominator.

$$\therefore \frac{p^0 - p}{p} = \frac{n_2}{n_1}$$

This is known as "Condensed Raoult's Law"

Derivation of Raoult's law :

According to Raoult's law, "The vapour pressure of a solvent in an ideal solution is equal to its mole fraction (x_1) multiplied by the vapour pressure of the solvent (P^0)".

$$P = x_1 P^0 \quad (1)$$

$$x_1 + x_2 = 1$$

$$x_1 = 1 - x_2 \quad (2)$$

Substitute (2) in (1),

$$P = (1 - x_2) P^0$$

$$\frac{P}{P^0} = (1 - x_2)$$

$$x_2 = 1 - \frac{P}{P^0}$$

$$\frac{P^0 - P}{P^0} = x_2$$

but

$$x_2 = \frac{n_2}{n_1 + n_2}$$

$$\frac{P^0 - P}{P^0} = \frac{n_2}{n_1 + n_2}$$

when compared to n_2 , n_1 is greater,

$n_2 \ll n_1$, then we neglected n_2 from the denominator

$$\frac{P^0 - P}{P^0} = \frac{n_2}{n_1}$$

$$\frac{P^0 - P}{P^0} = \frac{w}{mw} \times \frac{Mw}{W}$$

$$\frac{P^0 - P}{P^0} = \frac{w}{mw} \times \frac{Mw}{W}$$

Deviations of Raoult's Law:

- 1) Raoult's law is applicable only to very dilute solutions, which approximate to the ideal behaviour.
- 2) Raoult's law is applicable to solutions containing non-volatile solute only.
- 3) Raoult's law is not applicable to solutes which dissociate or associate in the particular solution.

PROBLEMS

Ex. 4) When a solution of sugar is prepared in water at 20°C , the vapour pressure of water (17.51 mm). Increased by 0.0614 mm. Calculate

- (i) RLVP (ii) vapour pressure of the solution (iii) Mole fraction of water and sugar solution?

Sol:

$$P^{\circ} = 17.51 \text{ mm}$$

Lowering of vapour pressure $P^{\circ} - P = 0.0614 \text{ mm}$.

(i) Relative lowering of vapour pressure = $\frac{P^{\circ} - P}{P^{\circ}}$

$$= \frac{0.0614}{17.51}$$

$$= 0.00351$$

$$= 0.00351$$

(ii) vapour pressure of the solution $P = P^{\circ} - (P^{\circ} - P)$

$$= 17.51 - 0.0614$$

$$= 17.4486 \text{ mm}$$

(iii) Calculation of mole fraction of the solute,

$$\frac{P^{\circ} - P}{P^{\circ}} = X_2$$

$$0.00351 = X_2 (\text{sugar})$$

$$\text{Hence, mole fraction of the solvent (water)} = 1 - 0.00351 \\ = 0.99649.$$

(Q2) The relative lowering of vapour pressure produced by dissolving 72 grams of substance in 1 kg of water is 0.009. What is the molecular mass of the substance?

Sol: RLVP = 0.009.

$$w = 72 \text{ gr} \quad W = 1 \text{ kg} = 1000 \text{ gr}$$

$$m_w = ? \quad M_w = 18$$

$$\frac{p^0 - p}{p^0} = \frac{w}{m_w} \times \frac{M_w}{W}$$

$$0.009 = \frac{72 \times 18}{m_w \times 1000}$$

$$m_w = \frac{72 \times 18}{0.009 \times 1000}$$

$$m_w = 144.$$

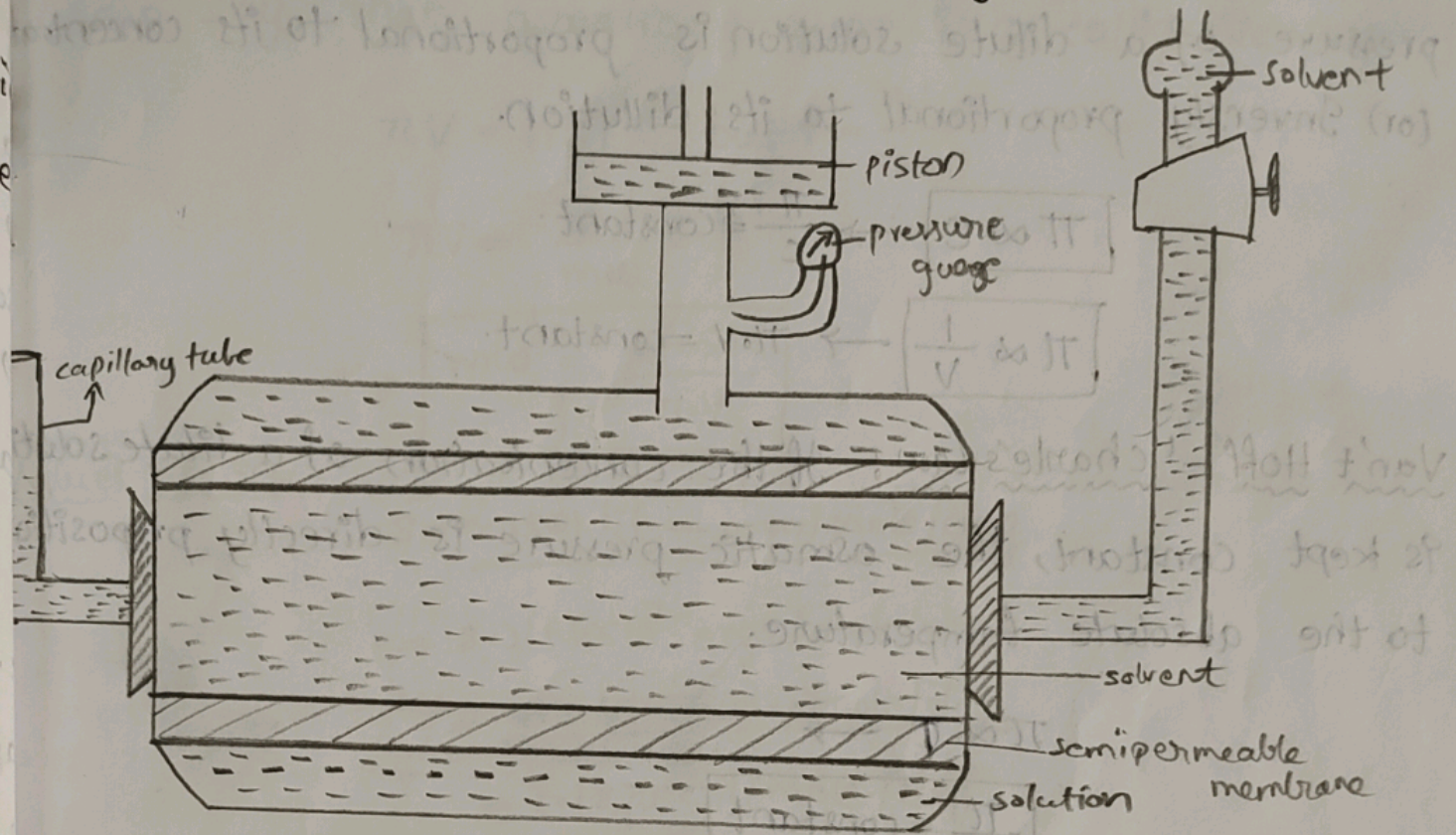
Osmotic pressure :

Osmosis :- "The phenomenon in which pure solvent molecules pass through a semi permeable membrane from a solution of lower concentration to a solution of higher concentration".

Osmotic pressure :- "The excess pressure which must be applied on a solution in order to prevent flow of solvent into the solution through the semi permeable membrane".

Isotonic solutions :- A pair of solutions having the same osmotic pressure are known as isotonic solutions. These solutions have the same molar concentration.

Measurement of osmotic pressure by Berkeley - Hartley's method:



This method involves the determination of the excess pressure that is applied upon the solvent to prevent the entry of the solvent into the solution.

The apparatus consists of a porous pot having electrolytically deposited copper ferro cyanide semi permeable membrane in its walls. On one side it is connected to capillary tube and to a dropping funnel on the other side. The porous pot is fitted into a gun metal jacket provided with an air-tight piston. This piston is attached to the pressure gauge. The porous pot is filled with the solution whose osmotic pressure is to be determined. The jacket is filled with solvent. Internal pressure is applied to the solution through the piston to prevent the entry of the solution. That pressure is known as osmotic pressure.

Von't Hoff - Boyle's Law: "At constant temperature the osmotic pressure of a dilute solution is proportional to its concentration (or) Inversely proportional to its dilution.

$$\boxed{\pi \propto C} \rightarrow \frac{\pi}{C} = \text{constant}$$

$$\boxed{\pi \propto \frac{1}{V}} \rightarrow \pi \cdot V = \text{constant}$$

Von't Hoff - Charles's Law: If the concentration of a dilute solution is kept constant, the osmotic pressure is directly proportional to the absolute temperature.

$$\pi \propto T \rightarrow$$

$$\boxed{\frac{\pi}{T} = \text{constant}}$$

General osmotic pressure for dilute solutions:

acc. to von't Hoff - Boyle's law, $\pi \propto \frac{1}{V}$

acc. to von't Hoff - Charles's law, $\pi \propto T$

combining both the laws, $\pi \propto \frac{1}{V} \propto T$

$$\pi \propto \frac{T}{V}$$

$$\pi V = ST$$

S = solution
T = temperature

for 'n' moles, $\boxed{\pi V = nST}$ Von't Hoff Equation

$$\pi = \frac{n}{V} \cdot ST$$

$$\pi = CST$$

since, the osmotic pressure of a solution at any given temperature T, depends upon the no. of moles per unit volume

and independent of the the nature of the solvent. Hence, we can say that osmotic pressure is a colligative property.

$$\pi V = nST \quad \text{but } n = \frac{W}{mw}$$

$$\pi V = \frac{W}{mw} S \cdot T$$

$$\boxed{mw = \frac{W \cdot S \cdot T}{\pi \cdot V}}$$

Values of S:

$$S = 0.0821 \text{ lit} - \text{atm/mole/deg.}$$

$$= 8.3160 \times 10^7 \text{ ergs/mole/deg}$$

$$= 8.3160 \text{ Joules/mole/deg}$$

$$= 1.9870 \text{ cal/mole/deg.}$$

PROBLEMS

Ex: 1) Calculate the osmotic pressure of 0.01M solution of urea at 300K. (S = 0.0821 lit - atm/deg/mole)

sol: $C = 0.01M = 0.01 \text{ moles lit}^{-1}$

$$S = 0.821 \text{ lit} - \text{atm deg}^{-1} \text{ mole}^{-1}$$

$$T = 300K.$$

$$\pi = CST$$

$$\pi = 0.01 \times 0.821 \times 300$$

$$= 0.2463 \text{ atm}$$

Ex: 2) Calculate the osmotic pressure of a 10% solution of cane sugar at 25°C. (R = 8.31 JK⁻¹ mole⁻¹)

sol: 10% solution of cane sugar means that it contains 10 gm of cane sugar per 100cc of the solution.

$$w = 10 \text{ gr}$$

$$mw = 342$$

$$V = 100 \text{ c.c.} = \frac{1}{10} \text{ lit}$$

$$S = 8.31 \text{ J. deg}^{-1} \text{ mole}^{-1}$$

$$T = 25 + 273 = 298 \text{ K. } \pi = ?$$

acc. to von't Hoff. Equation,

$$\pi V = n S T$$

$$\pi V = \frac{w}{mw} \cdot S \cdot T$$

$$\pi = \frac{w}{mw} \times \frac{S T}{V}$$

substituting the values in the equation.

$$\pi = \frac{10}{342} \times \frac{8.31 \times 298 \times 10}{1}$$

$$= 724.09 \text{ J.}$$

Elevation in Boiling point: Boiling point of a liquid is defined as the temperature at which its vapour pressure is equal to atmospheric pressure. Elevation in the boiling point of the solvent is due to the addition of a non-volatile solute. This can be readily understood from the vapour pressure curves of pure solvent.

If the boiling point of a pure solvent is given and if a small amount of non-volatile solute is added to this solvent, then the B.P. of the solution will be greater than that of the pure solvent.

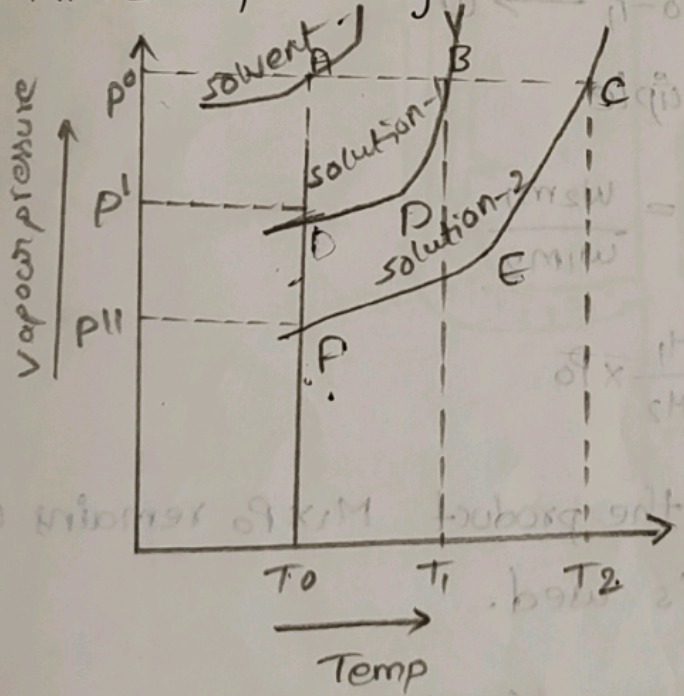
Let us consider the B.P. of the solution is T , the elevation

in boiling point is $\Delta T_b = T - T_0$.

We should know that as the vapour pressure of any solution decreases its boiling point increases, when solute is added to the solvent it ↓ses the vapour pressure. Hence boiling point ↑ses. The increase in B.P by addition of non-volatile solute to a solvent is known as elevation of boiling point.

consider a pure solvent, solution-I and solution-II in which the conc. of solution-II is greater than solution-I. If a graph is drawn between the vapour pressure and boiling points of these systems the curves formed are as shown in fig.

Let us consider T_0, T_1, T_2 are the boiling points of solvent, solution-I, solution-II. the corresponding vapour pressures are P_0, P_1, P_2 respectively.



→ In the diagram, the curves BD and EF are parallel lines for the given systems. Hence the triangles ACF & ADB are equal triangles then,

$$\frac{AC}{AB} = \frac{AF}{AD}$$

from the diagram

$$AC = T_2 - T_0$$

$$AB = T_1 - T_0$$

$$AF = P_0 - P_2$$

$$AD = P_0 - P_1$$

- Boiling point of pure solvent = T_0
- Boiling point of solution-I = T_1
- Boiling point of solution-II = T_2

$$\text{then, } \frac{T_2 - T_0}{T_1 - T_0} = \frac{P_0 - P_2}{P_0 - P_1}$$

$$\frac{\Delta T_2}{\Delta T_1} = \frac{\Delta P_2}{\Delta P_1}$$

$$\frac{\Delta T_2}{\Delta P_2} = \frac{\Delta T_1}{\Delta P_1}$$

$$\frac{\Delta T}{\Delta P} = K (\text{constant})$$

From this the boiling points of different systems are directly proportional to the lowering of vapour pressure

$$\Delta T_b \propto P_0 - P$$

Determination of Molecular weight of solute by elevation boiling point:

$$\text{We know that } \Delta T_b \propto P_0 - P_1 \rightarrow \textcircled{1}$$

from Raoult's principle

$$\frac{P_0 - P}{P_0} = \frac{n_2}{n_1 + n_2} = \frac{w_2 M_1}{w_1 M_2}$$

$$\text{then } P_0 - P = \frac{w_2 M_1}{w_1 M_2} \times P_0$$

In the above equation, the product $M_1 \times P_0$ remain constant when the same solvent is used.

$$P_0 - P = \frac{w_2}{w_1 \times M_2} \times \text{constant}$$

$$\therefore P_0 - P \propto \frac{w_2}{w_1 \times M_2} \rightarrow \textcircled{2}$$

from eq $\textcircled{1}$ & $\textcircled{2}$

$$\Delta T_b \propto \frac{w_2}{w_1 \times M_2} \quad \text{Then } \Delta T_b = K_b \times \frac{w_2}{w_1 \times M_2}$$

where K_b = molar elevation constant.

To define K_b consider $\frac{W_2}{M_2} = 1 \text{ mole}$ & $W_1 = 1 \text{ kg}$ then

$$\Delta T_b = K_b$$

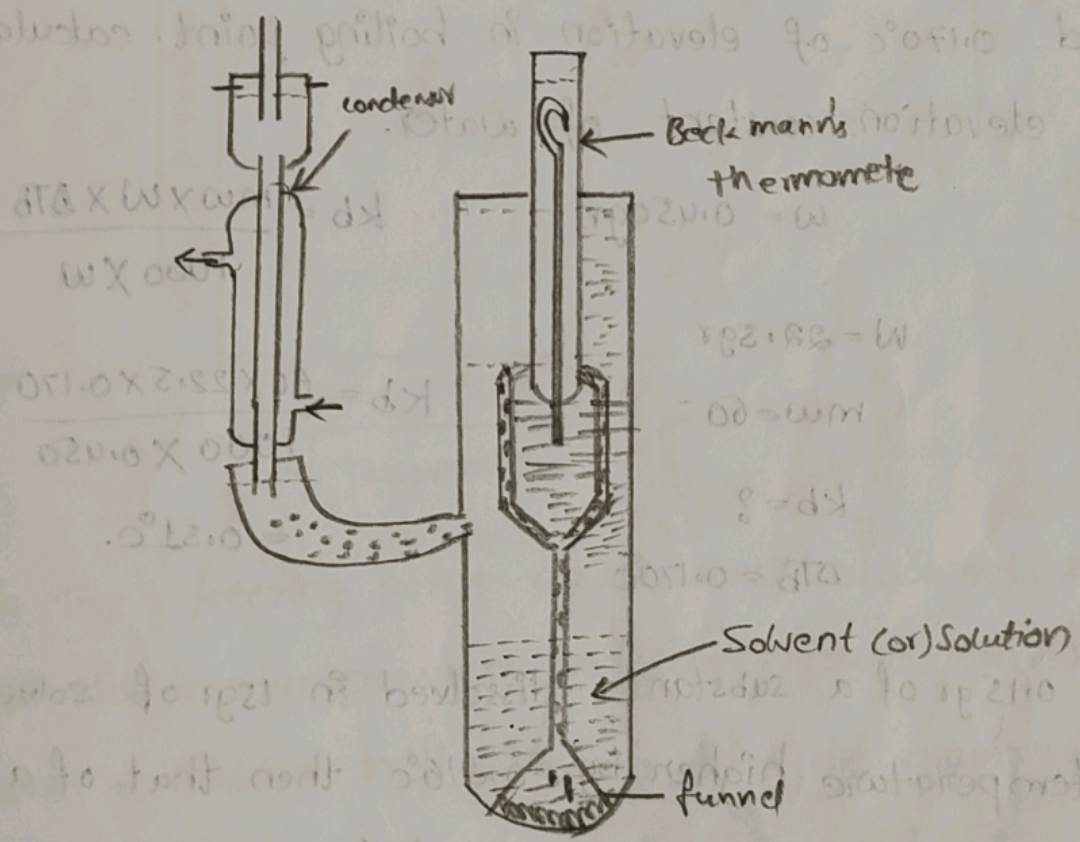
K_b = Molar elevation constant.

If the weight of the solvent is given in gms.

$$\text{then } \Delta T_b = \frac{K_b \times W_2 \times 1000}{W_1 \times M_2}$$

$$\therefore M_2 = \frac{K_b \times W_2 \times 1000}{W_1 \times \Delta T_b}$$

Determination of elevation of boiling point by Cottrell's method:-



Cottrell's apparatus consists of graduated boiling tube containing solvent or solution, a condenser fitted. In the side tube of the main graduated tube, the condenser returns the vapourised solvent to the boiling tube.

Solvents is placed in the boiling tube having a few fragments of a porous pot below the mouth of the funnel. The tube is heated on a small flame. Now, the temperature reached is exactly that of the boiling liquid and the super heating is minimum, this is the B.P. of the pure solvent.

Now, weighed amount of the solute is added to the solvent and boiling point of the solution is determined as that of the solvent.

PROBLEMS

Ex: 1) A solution of 0.450 gr. of urea (m.wt = 60) in 22.5 of water showed 0.170°C of elevation in boiling point. calculate the molal elevation constant of water.

sol:

$$w = 0.450 \text{ gr}$$

$$k_b = \frac{m_w \times W \times \Delta T_b}{1000 \times w}$$

$$W = 22.5 \text{ gr}$$

$$m_w = 60$$

$$k_b = ?$$

$$\Delta T_b = 0.170^{\circ}\text{C}$$

$$k_b = \frac{60 \times 22.5 \times 0.170}{1000 \times 0.450}$$

$$= 0.51^{\circ}\text{C}$$

Ex: 2) 0.15 gr of a substance dissolved in 15 gr of solvent boiled at a temperature higher by 0.216°C than that of a pure solvent. calculate the molecular weight of the substance ($k_b = 2.16^{\circ}\text{C}$)

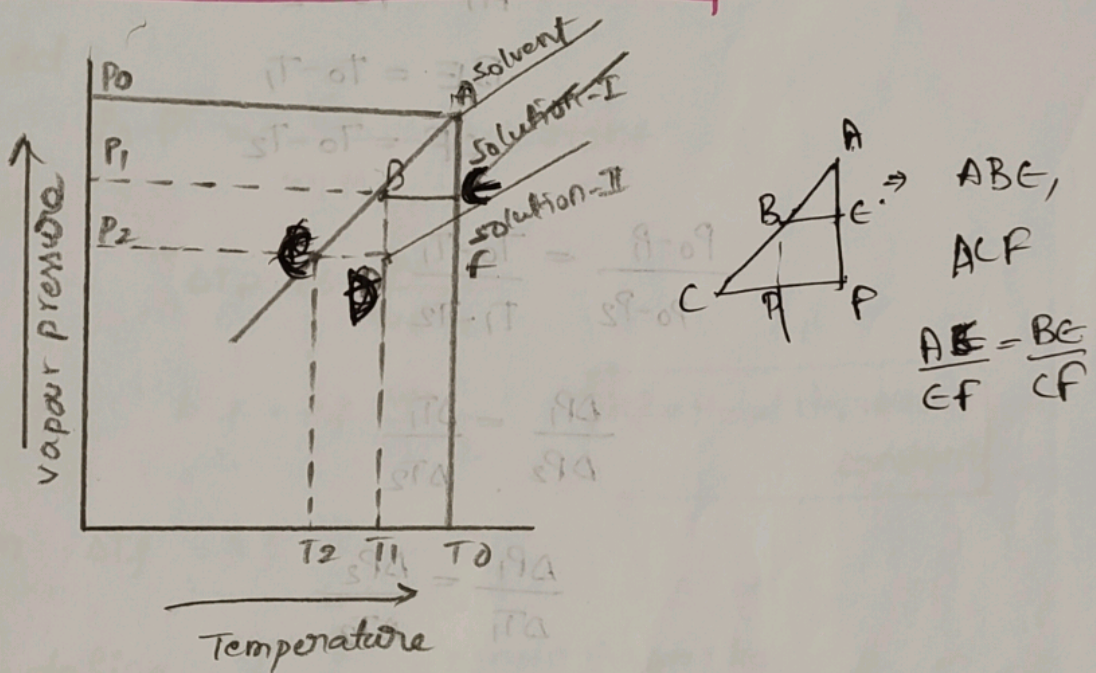
sol: Depression in freezing point:

Freezing point is the temperature at which the liquid and the solid states of a substance are in equilibrium with each other.

the vapour pressure of a liquid is lowered by the addition of a non-volatile solute. In other words freezing point of a solution will be lower than the freezing point of the pure solvent.

T_0 is the freezing point of pure solvent and T is the freezing point of the solution. The difference in the two freezing points are called the depression in freezing point which is denoted by ΔT_f .

Depression in freezing point $\Delta T_f = T_0 - T$



Study the freezing point curves, consider ^{the} solvent, solution-I solution-II. The vapour pressure and temperature curves of this systems are as shown in the graph. from the graph point A represents the equilibrium btw solid and liquid of pure solvent. Similarly the points B & C represents the freezing points of solution-I & solution-II. Let us consider P_0, P_1, P_2 are the vapour pressures of pure solvent, solution-I & solution-II.

similarly T_0, T_1, T_2 are the freezing points of solvent, solution
solution π .

* For a very dilute solutions BE and CF are parallel lines.
Hence the triangles ABE & ACF are equal triangles.

$$\triangle ABE = \triangle ACF$$

$$\text{Then } \frac{AE}{AF} = \frac{BE}{CF}$$

From graph,

$$AE = P_0 - P_1$$

$$AF = P_0 - P_2$$

$$BE = T_0 - T_1$$

$$CF = T_0 - T_2$$

$$\frac{P_0 - P_1}{P_0 - P_2} = \frac{T_0 - T_1}{T_1 - T_2}$$

$$\frac{\Delta P_1}{\Delta P_2} = \frac{\Delta T_1}{\Delta T_2}$$

$$\frac{\Delta P_1}{\Delta T_1} = \frac{\Delta P_2}{\Delta T_2}$$

$$\therefore \frac{\Delta P}{\Delta T} = \text{constant}$$

$$\therefore \boxed{\Delta T_f \propto P_0 - P}$$

The temperature in freezing point is directly proportional
to lowering of vapour pressure.

Determination of Molecular weight of solute from depression
in freezing point:

From the graph, we know that

$$\Delta T_f \propto P_0 - P \rightarrow (1)$$

From Raoult's law

$$\frac{P_0 - P}{P_0} = \frac{w_2 M_1}{w_1 M_2} \rightarrow (2)$$

$$P_0 - P = \frac{w_2 M_1}{w_1 M_2} \times P_0$$

from (1) & (2)

$$\Delta T_f = \frac{w_2 M_1}{w_1 M_2} \times P_0$$

The product of $M_1 P_0$ remains constant, when the same solvent is used

$$P_0 - P = \frac{w_2}{w_1 M_2} \times \text{constant}$$

$$\Delta T_f \propto \frac{w_2}{w_1 M_2}$$

$$\Delta T_f = k_f \frac{w_2}{w_1 M_2}$$

k_f = Molal depression constant

$$\text{Then } \Delta T_f = k_f \frac{w_2}{w_1 M_2}$$

to define it $\frac{w_1}{M_2} = 1 \text{ mole} \ \& \ w_1 = 1 \text{ kg}$

$$\text{Then } \Delta T_f = k_f$$

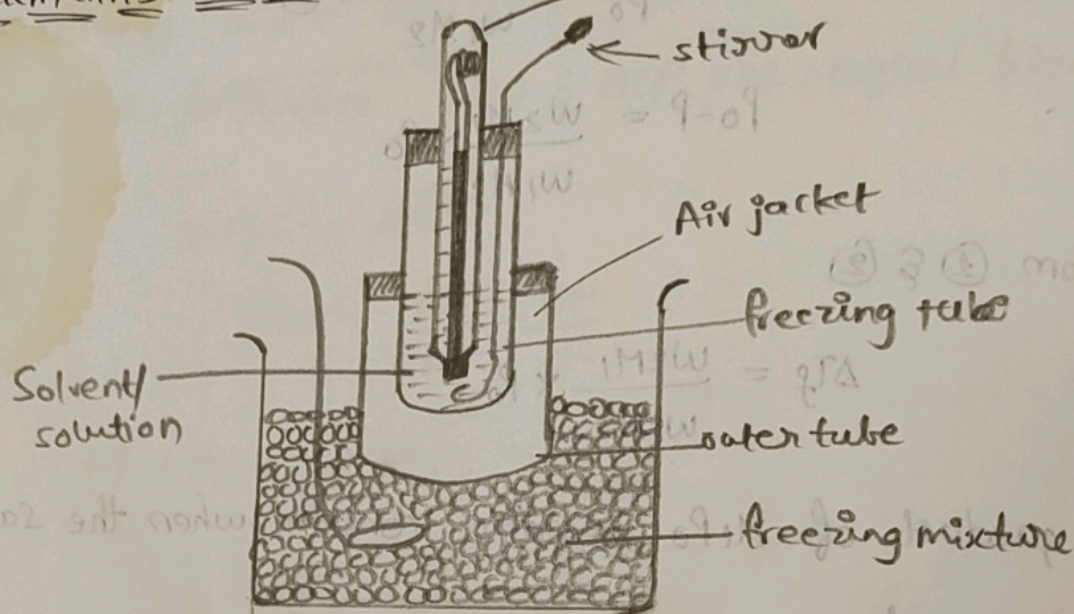
$$\therefore M_2 = \frac{k_f w_2}{w_1 \Delta T_f}$$

If the weight of the solvent is given in gms.

$$\text{then, } M_2 = k_f \cdot \frac{w_2 \times 1000}{w_1 \times \Delta T_f}$$

(21) Determination of Freezing point depression

↳ Beckmann's method :- Beckmann's thermometer



The inner freezing tube fitted with a Beckmann thermometer and a platinum stirrer. The outer glass tube which is fitted the inner freezing tube, leaving an air space between them. A glass jar containing a suitable freezing mixture whose F.P. is about 5°C lower than that of the pure solvent.

Take a known weight of the pure solvent in the freezing tube and suspended the thermometer in the freezing tube. Report the F.P. of a pure solvent. Now, add non-volatile solute to the solvent and Report the F.P. of solution. The difference between them is called depression in F.P.

PROBLEMS

Ex: 1) 0.750gr of a compound A dissolved in 25gr. of the solvent lowered the F.P. of the solvent by 0.502°C . Calculate the m.wt of the substance. The molecular depression constant of the solvent is 50.2°C per 10gr of the solvent.

$$w = 0.750 \text{ gr} \quad \Delta T_f = 0.502^\circ\text{C} \quad W = 25 \text{ gr} \quad (17)$$

$$k_f = 50.2^\circ\text{C per } 100 \text{ gr}$$

$$m_w = ?$$

$$m_w = \frac{100 \times k_f \times w}{\Delta T_f \times W}$$

$$= \frac{100 \times 50.2 \times 0.750}{0.502 \times 25}$$

$$m_w = 300$$

calculate the FOP of 1% solution of glucose in water, given that molal depression constant for water is $1.84 \text{ K. mole}^{-1}$.

$$w = 1 \text{ gr}$$

$$W = 99 \text{ gr}$$

$$m_w = 180$$

$$k_f = 1.84$$

$$\Delta T_f = \frac{1000 \cdot k_f \cdot w}{m_w \times W}$$

$$= \frac{1000 \times 1.84 \times 1}{180 \times 99}$$

$$= 0.1032^\circ\text{C}$$

$$\text{Freezing of the solution} = F_{\text{no. of solvent}} - \Delta T_f$$

$$= 0 - 0.1032^\circ\text{C}$$

$$= -0.1032^\circ\text{C}$$

Abnormal behaviour of solutions :-

Since, the colligative properties of solutions depend on the no. of solute particles present in solution and not on their nature, colligative properties of the solutes which undergo dissociation in solution would be higher than expected for the non-electrolytes.

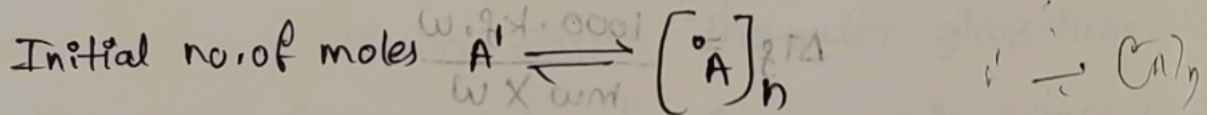
Van't Hoff factor (i) :- It can be defined as the ratio of observed colligative property to normal colligative property

$$i = \frac{\text{observed colligative property}}{\text{Normal colligative property}}$$

(or)

$$i = \frac{\text{Normal molecular weight}}{\text{observed molecular weight}}$$

Van't Hoff factor and Degree of Association :- The degree of association of a substance is defined as the fraction of the total no. of molecules of the substance which exist as associated molecules.



No. of moles after association $1 - \alpha + \frac{\alpha}{n}$

Total no. of moles after association = $1 - \alpha + \frac{\alpha}{n}$

Van't Hoff factor (i) = $\frac{\text{observed colligative effect}}{\text{Normal colligative effect}}$

$$i = \frac{1 - \alpha + \frac{\alpha}{n}}{1}$$

$$i = 1 - \alpha + \frac{\alpha}{n}$$

$$i = 1 - \alpha \left[1 - \frac{1}{n} \right]$$

$$\alpha = \frac{1 - i}{1 - \frac{1}{n}}$$

Van't Hoff factor and Degree of Dissociation: (18)

The degree of dissociation of a substance is defined as the fraction of the total no. of molecules which dissociate in the solution into simpler molecules.

1 mole of an electrolyte gives n number of ions.

α = degree of dissociation.

No. of undissociated molecules of the electrolyte = $1 - \alpha$

No. of ions produced due to dissociation = $n\alpha$

\therefore Total no. of particles after dissociation = $1 - \alpha + n\alpha$

$$i = \frac{\text{observed colligative effect}}{\text{Normal colligative effect}}$$

$$i = \frac{1 - \alpha + n\alpha}{1}$$

$$i = 1 - \alpha + n\alpha$$

$$i - 1 = \alpha(n - 1)$$

$$\alpha = 1 - \alpha(n - 1)$$

$$\alpha = \frac{i - 1}{n - 1}$$

$$i - 1 = \alpha(n - 1)$$

SHORT QUESTIONS

$$\alpha = \frac{i - 1}{n - 1}$$

1) state and explain the Raoult's law.

2) what is van't Hoff's factor and explain.

3) Explain about the abnormal colligative properties.

4) Explain about determination of depression of freezing point by Beckmann's method.

5) How can you determine the osmotic pressure by Berkeley-Quinley's method.

LONG QUESTIONS

(i) Derive an expression for depression of freezing point.

(ii) Derive an equation for elevation of boiling point.



No. of undissociated molecules of the electrolyte = $1 - \alpha$
No. of ions produced due to dissociation = $n\alpha$
∴ Total no. of particles after dissociation = $1 - \alpha + n\alpha$

$$i = \frac{\text{observed colligative effect}}{\text{Normal colligative effect}}$$

$$i = \frac{1 - \alpha + n\alpha}{1}$$

$$i - 1 = n\alpha - \alpha$$

$$\alpha = \frac{i - 1}{n - 1}$$

SHORT QUESTIONS

Explain about the abnormal colligative properties.
Explain about determination of depression of freezing point by Beckmann's method.
How can you determine the osmotic pressure by Berkeley's method.
Explain the vant Hoff's factor and explain the Raoult's law.